

Modelling and analysis of eddy current losses in permanent magnet machines with multi-stranded bundle conductors

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Abstract

This paper investigates the influence of eddy current losses in multi-stranded bundle conductors employed in out-runner permanent magnet machines, by adopting an analytical model. The analytical model is based on a sub-domain field model that solves the two-dimensional magnetostatic problem using the separation of variables technique for each of the non-magnetically permeable machine sub-domains: PM, airgap and slots. The validity and accuracy of the proposed model is verified using finite element analysis and then used to investigate the eddy current losses. The machine considered for the analysis has 36 slots and 42-poles previously designed for aircraft taxiing. The influence of the number of turns and the conductor cross-sectional area are investigated. It is shown that efficiency can be improved considerably by the choice of multi-stranded bundle conductors.

Keywords: AC Losses, analytical, eddy currents, proximity losses, permanent magnet, sub-domain field model

1. Introduction

Permanent magnet (PM) machines are being used extensively in diverse transportation applications due to the high torque density and subsequently high power density that they can achieve. Although such machines are designed to have high power density, the resultant losses including winding losses, iron losses and magnets' eddy current losses are inevitable. To diminish these losses and thus improve the overall efficiency, several actions can be taken at the design stage, namely:

1. Laminated material and segmented magnets are used to reduce eddy current losses in the iron and the magnets, respectively;
2. Materials that have a better magnetic properties are preferred to avoid magnetic losses;
3. Magnetic material with high resistivity to reduce iron losses;
4. Litz conductor or multi-stranded bundle conductors are used to diminish winding eddy current losses.

Here, it is worth highlighting that although the application of Litz wire/ multi-stranded bundle conductor significantly limits the effects of eddy current losses due to skin effect [1, 2], the winding eddy losses due to the proximity effect still persists. In addition direct current (DC) winding losses also increase due to the poor fill factor of the Litz wire/ multi-stranded bundle conductors. However, considering that these losses can be minimized, and then, there is still much to gain by implementing a Litz wire/ multi-stranded bundle conductor.

In literature, proximity losses are researched thoroughly and methods for reducing them are presented where it has been reported that these losses can be reduced by an appropriate winding arrangement in the slot [6]. Alternative analytical methods [1, 3, 5, 7] are also proposed to predict proximity losses within acceptable accuracy and less computation time. But, the influence of the number of strands and the strand cross-sectional area of the Litz/ multi-stranded conductor is not reported. This all indicates that the choice of the conductors' number/cross-sectional area of Litz wire becomes an important factor to consider during the design stage, in order to balance the alternating current (AC) losses and their DC counterpart.

In this paper, the influence of eddy current losses in multi-strand bundle conductors employed in an out-runner, PM machine used for aircraft taxing [4] is investigated adopting an analytical model. The machine considered for the analysis is a 36-slot/ 42-pole with an outer rotor. The analytical model is based on a sub-domain field model that solves the two-dimensional problem using the separation variables technique for each of the non-magnetically permeable machine sub-domains: PM, airgap and slots. The validity and accuracy of the proposed model is verified using finite element (FE) analysis and then used to investigate proximity losses. The influence of the number of turns and conductor cross-sectional area is then investigated. It is shown that the efficiency can be improved considerably at the design stage by an appropriate choice of conductors.

2. Analytical model

It is well known that the use of FE method in the prediction of the eddy current losses in slot's conductors requires a significantly large mesh. Indeed, creating the FE model consists of individual conductors and solving are highly time-consuming. Analytical models which provide the complementary solution can be an alternative for analyzing the eddy current losses. The analytical methods are not only faster than FE, but also provide insight into the field computations. Herein, analytical model is therefore considered to analyze the eddy current losses. The adopted analytical method is based on field model which divide the field domain into several simple sub-domain and solve the potential expression in each sub-domain.

To compute the field in each sub-domain, the cross-sectional area of the machine which is the field domain, is therefore divided into three sub-domains: rotor PM sub-domain (A_I – region I), air gap sub-domain (A_{II} – region II), and slot sub-domain (A_i – region III) as shown in Fig.1b where, A represents the Z-component of the magnetic vector potential.

The machine considered for the study has Q number of open slots and each slot is represented with subscripts i . The angular position of the i^{th} slot is defined as

$$\theta_i = -\frac{\beta}{2} + \frac{2\pi i}{Q} \quad \text{with } 1 \leq i \leq Q \quad (2.1)$$

where β is the slot angle and the other geometric parameters are represented in Fig.1. The modelling paradigm assumes:

1. the machine has a radial geometry as shown in Fig.1;
2. the stator and rotor cores have an infinite permeability and zero conductivity;
3. the magnets are magnetized in the radial direction and their relative recoil permeability is unity ($\mu_r = 1$);
4. the end-effects are neglected and thus the magnetic vector potential has only one component along the z direction and it only depends on the polar coordinates r and θ ;
5. the walls of the slot are finely laminated so that the effect of eddy currents within the iron can be neglected.

The magnetostatic partial differential equations governing in the different sub-domains derived from Maxwell's equations and formulated in terms of vector potential are:

$$\begin{cases} \frac{\partial^2 A_I}{\partial r^2} + \frac{1}{r} \frac{\partial A_I}{\partial r} + \frac{1}{r^2} \frac{\partial^2 A_I}{\partial \theta^2} = \frac{-\mu_o}{r} \frac{\partial M_r}{\partial \theta} \\ \frac{\partial^2 A_{II}}{\partial r^2} + \frac{1}{r} \frac{\partial A_{II}}{\partial r} + \frac{1}{r^2} \frac{\partial^2 A_{II}}{\partial \theta^2} = 0 \\ \frac{\partial^2 A_i}{\partial r^2} + \frac{1}{r} \frac{\partial A_i}{\partial r} + \frac{1}{r^2} \frac{\partial^2 A_i}{\partial \theta^2} = -\mu_o J \end{cases} \quad (2.2)$$

Thus, the general solution can be obtained by employing the separation of variables method in each sub-domain. Details of the solution of equation (2.2) can be found in [5].

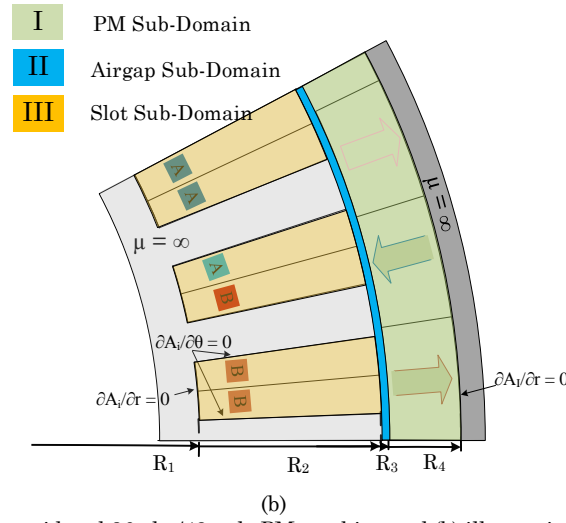
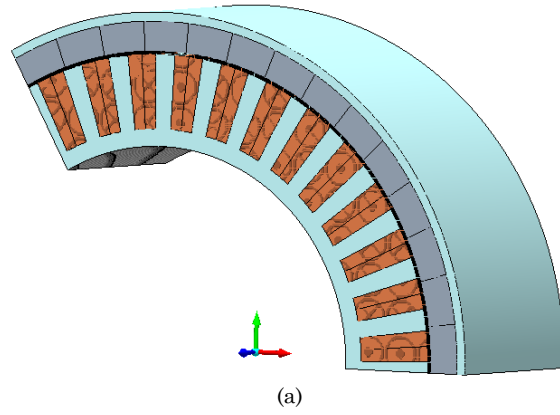


Fig.1. (a) 1/3 cross sectional view of the considered 36-slot/42-pole PM machine and (b) illustration of sub-domains regions and their associated boundary conditions

3. Proximity losses evaluation

In order to predict the eddy current losses in each conductor the magnetic vector potential obtained in the slot sub-domain is used. Here, an assumption is made that the winding conductors are designed to have a diameter less than the skin depth δ at the nominal operating frequency (63 Hz), and thus the induced eddy current density (J_e) in the conductors is only resistance limited. The maximal conductor depth δ_m that satisfies the above assumption is evaluated using the classical skin depth equation:

$$\delta_m = \sqrt{\frac{2}{\sigma \omega \mu_r \mu_0}} \quad (3.1)$$

where, ω is the electrical frequency, μ_r and σ are the relative permeability and the conductivity of the conductors material (in this case, it is copper), respectively; $\mu_r = 1$; $\sigma = \sim 5.77 \times 10^7$ S/m.

Hence, the resultant eddy current density J_e in the conductor due to eddy current effect [1] can be expressed as shown in equation (3.2)

$$J_e = -\sigma \frac{\partial A_t}{\partial t} + C(t) \quad (3.2)$$

where, C is a time dependent constant introduced in order to ensure that the total current flowing through each conductor is equal to the source current [1], The power over a fundamental electrical period in a conductor can thus be obtained by

$$P = \frac{\omega l_{stk}}{2\pi\sigma} \int_0^{2\pi/\omega_o} \int_{r_{c1}}^{r_{c2}} \int_{\theta_{c1}}^{\theta_{c2}} (J_e + J)^2 r d\theta dr dt \quad (3.3)$$

where, l_{stk} is active axial length of the conductor and r_{c1} , r_{c2} , θ_{c1} , θ_{c2} are the inner and outer radius of the conductor and the angular position of the conductor tangential extremities, respectively.

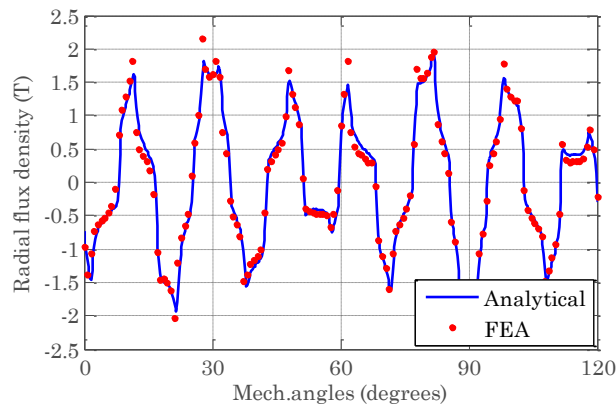
Table 1
Specification of the PM machine

Design parameters	
R ₁	153.5 mm
R ₂	203.5 mm
R ₃	205.5 mm
R ₄	225.5 mm
Slot angle (β)	5.9 mech.degrees
Axial length (l_{stk})	151 mm
Number of turns per coil	33
Cross section area of a conductor	7.84 mm ²
Current density in the slot (J)	16.05 A/mm ²
Remanence flux density of the PM (B_r)	1.02 T
Nominal speed	180 rpm
Output power	132 kW

4. Model verification via FE analysis

An FE model of the 36-slot/42-pole machine is built and used to validate the analytical model. The main parameters and specifications of the machine are presented in Table I. In the FE analysis a similar radial geometry as for the analytical model is considered, while the soft magnetic material is assumed to have a linear permeability characteristic. In order to compute the eddy current losses, the conductors are placed individually in the slot and connected in series to form a coil. In the design, rectangular conductor arrangement is adopted to improve the fill factor. Herein, a fill factor of 0.61 is achieved.

Fig.2 and Fig.3 show the radial and tangential components of flux density in the middle of the airgap ($r = 204.5\text{mm}$) and the slot ($r = 178.5\text{mm}$) respectively. The results obtained have a good agreement with the FE ones.



(a)

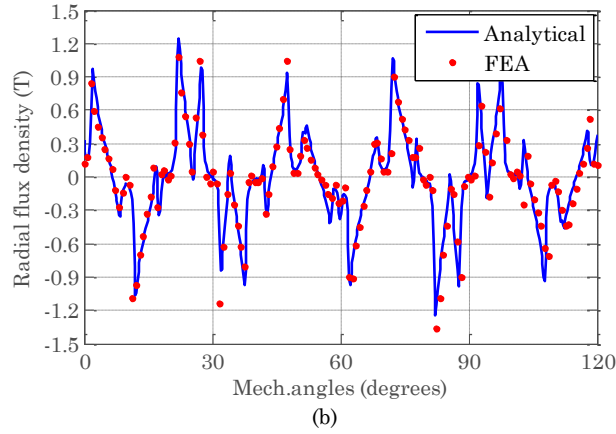


Fig.2. (a) Radial (b) tangential flux density in the middle of the airgap ($r = 204.5$ mm)

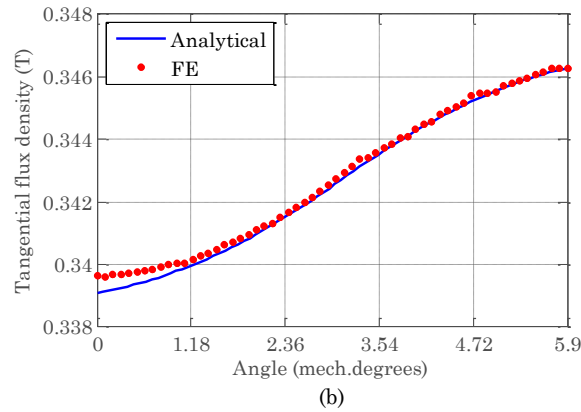
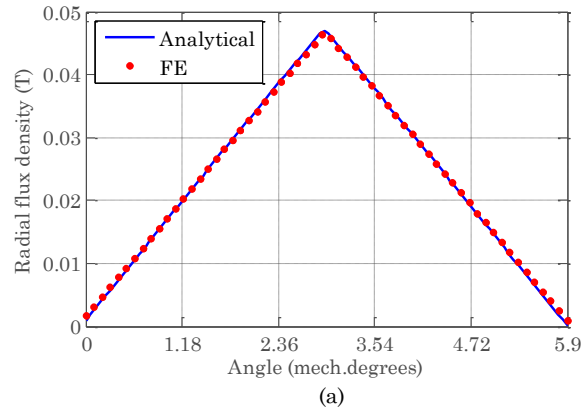


Fig.3. (a) Radial (b) tangential flux density in the middle of the slot-domain ($r = 178.5$ mm)

Fig.4 shows the comparison between the analytically and the FE calculated winding losses in a coil under no-load ($J = 0$; $B_r = 1.02$ T) and also on peak load ($J = 16.05$ A/mm²; $B_r = 1.02$ T) conditions, respectively. The obtained results are shown in Fig.4 to be in a good agreement. For a given operating speed, the computation time for loss estimation is about 1.7 s with the analytical model whereas the FE takes about 6.2 minutes.

From Fig.4b, it can also be seen that there is a difference (4% - 11%) at frequencies over ~ 80 Hz (apparition of skin effect). Using equation (3.1), it can be shown how, for example, for a fundamental operating frequency of 63Hz the maximal skin depth is 8.33 mm; In this case, the conductor has an area of 7.84 mm² (5.6 mm length and 1.4 mm width). All this indicates that for frequencies lower than 80Hz the conductor is only subject to proximity losses.

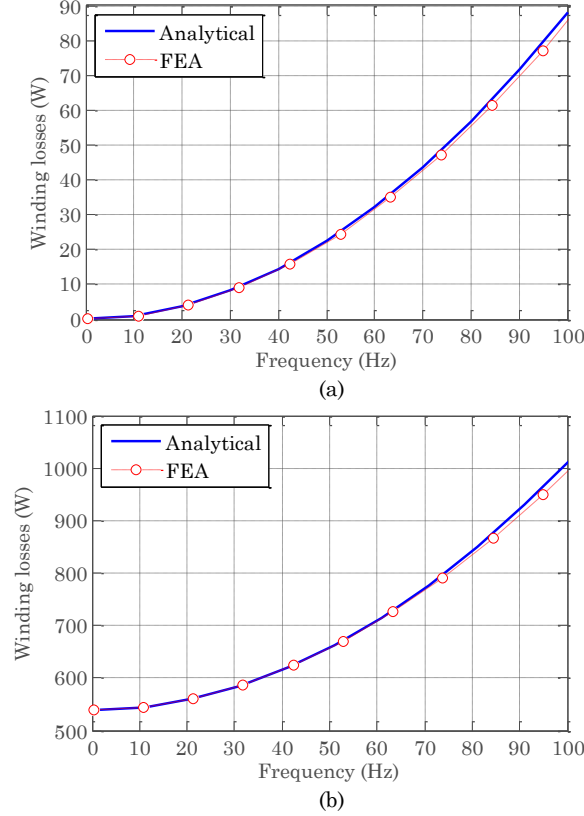


Fig.4. Winding losses in a coil at (a) no-load ($J_c = 0$; $B_r = 1.02T$) and (b) load ($J_c = 16.05 \text{ A/mm}^2$; $B_r = 1.02T$) conditions.

From Fig.4 it also can be seen that the analytically calculated results are slightly higher than the FE calculated ones at frequencies higher than 80Hz although eddy current reaction effect is considered in FE computation. This is due to the role of eddy current and their reaction effect that change the current distribution within the conductor resulting in a decrease of eddy current losses [3]. It is worth noting that this reaction effect depends on the size and structure of the conductor [2].

From the results it also can be seen that the winding AC losses which include both DC losses and eddy current losses, are 35% higher than DC losses at nominal speed of 180 rpm (63Hz). As a result the overall efficiency drops by 4.9% if the eddy current losses are not considered in the design stage.

A method by which to diminish these eddy current losses is the implementation of Litz or multi-strand bundle conductors. However this comes at the cost of a further increase in DC losses, automatically reducing the overall efficiency. A comparative exercise in order to define the optimal balance between the AC losses and DC losses is thus done and this is presented in the following section.

5. Proximity losses investigation in multi-stranded bundle conductors

In this section, the proximity losses and their influence on machine's efficiency are investigated for various multi-stranded bundle conductors with different cross-sectional areas and number of turns. For clarity of reading, parallel conductors and conductor that includes a number of parallel conductors are referred to as sub-stand and bundle conductor (see Fig.5) throughout this section. The losses are investigated for nine cases in which the turns' number of bundle conductors is kept constant (33 turns per coil), but the number of sub-strands associated to a bundle are varied from one to nine to identify the changes in the current distribution and their influences on the total winding losses. A sub-strand for a bundle is the original design and others are considered alternative.

The analysis is carried out using the analytical field model presented in section 2 where an assumption is made that the considered bundle conductor has its parallel turns not twisted or transposed. So, the winding losses associated with the machine depend only on the arrangement of the sub-strands in a bundle conductor. Also, it is worth noting that since a bundle has a number of sub-strands which are not twisted or transposed, the different sub-strands of the bundle conductor would not carry the same fraction of the

current. In the losses computation, the current flow in each sub-strand is therefore accounted for individually in the post processing stage by introducing the total current flow in the sub-strands as functions of inductance variation.

For the losses computation, the fill factor for each configuration of bundle conductor is evaluated assuming the slot is filled with a fill factor K_f (See Table 2). In the fill factor evaluation, insulation thickness of each strand in the bundle conductor and the slot wall insulation are assumed to be identical. For each configuration both DC losses and AC losses are calculated at rated operation. The obtained results are given in Fig.6.

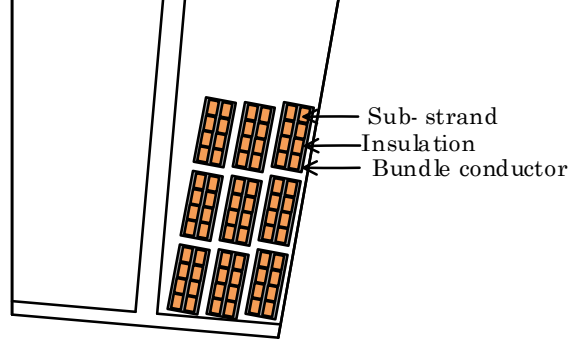


Fig. 5. An illustration of the bundle conductors and its sub-strands within a slot (8 sub-strands per bundle here)

TABLE 2

FILL FACTOR EVALUATION FOR DIFFERENT BUNDLE ARRANGEMENTS

Description	Fill factor (K_f)
33 bundle conductors and 1 sub-strand per bundle	0.61
33 bundle conductors and 2 sub-strand per bundle	0.52
33 bundle conductors and 4 sub-strand per bundle	0.46
33 bundle conductors and 8 sub-strand per bundle	0.41

It can be clearly seen that as expected the DC losses increase as the sub-strands in a bundle conductor increases. The AC losses initially reduce and then increase as the sub-strands in the bundle conductor increases. This is mainly due to the reduction in eddy current losses whilst the DC losses increase with the winding fill factor decreasing. Also it is worth noting that the efficiency of the machine is influenced by the number of sub-strands. The efficiency is improved by 1.5% when employing two sub-strands within a bundle. This confirms that utilizing a sub-strand configuration influences the current distribution in the slot and thus, efficiency can be improved if sub-strands are properly adopted.

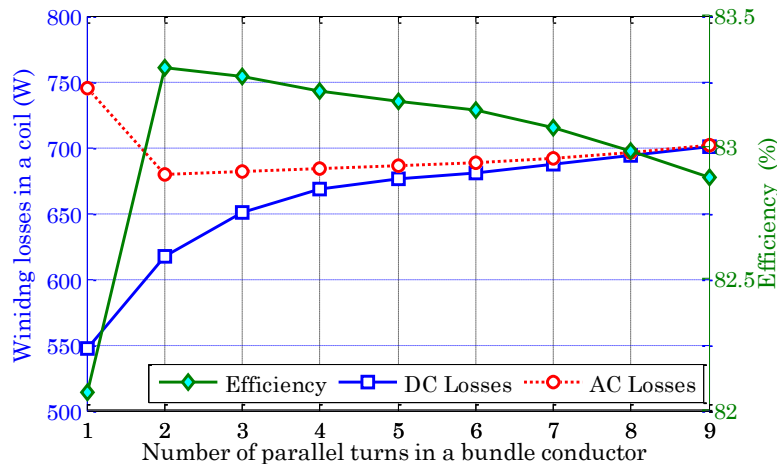


Fig.6. AC and DC losses vs. number of conductors in bundle conductors

Although adopting two parallel conductors per turn improves the efficiency, reduced fill factor and increased insulation may influence the temperature in the slot. It may further require oversized cooling arrangement within the machine. In order to confirm this, thermal analysis is carried out for two different configurations under similar conditions: 33 bundle conductors and 1 sub-strand per bundle and 33 bundle

conductors and 2 sub-strands per bundle. The thermal analysis is carried out using 2D FE. The analysis is done at rated conditions where the previous analytically calculated AC losses are used. The temperature distributions in the slot for associated losses are presented in Fig.7.

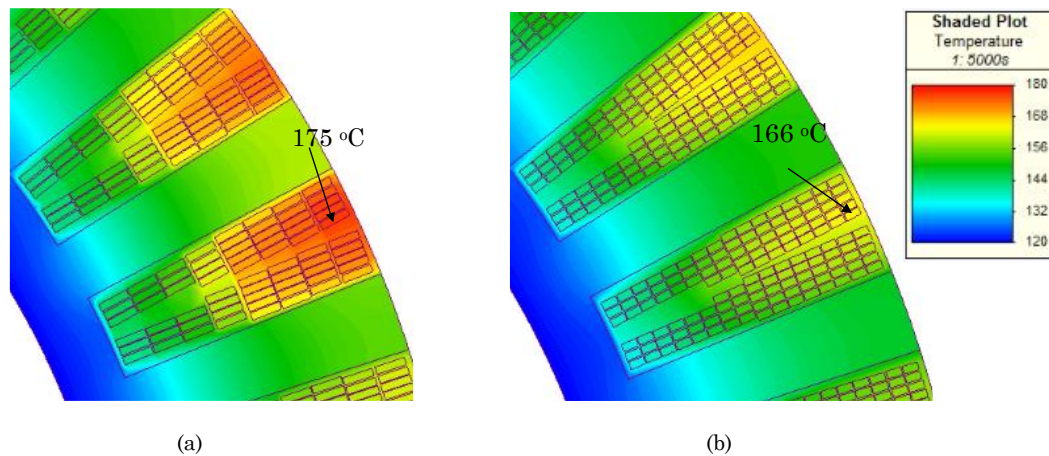


Fig.7. Temperature distribution of (a) 33 bundle conductors and 1 sub-strand and (b) 33 bundle conductors and 2 sub-strands

From the results, it is evident that the application of two parallel conductors per turn significantly reduces the losses without affecting the cooling arrangement of the design; also it reduces the slot temperature compared to the initial design of the machine. Hence, it can be concluded that the choice of the sub-strands number/cross-sectional area of a bundle conductor becomes an important factor which is necessary to consider during the design stage, in order to balance the AC losses and their DC counterpart. It is also worth highlighting here that the proximity losses can be reduced significantly due to current re-distribution of parallel conductors, although the transposition is not adopted.

5. Conclusion

In this paper, the influence of proximity losses in PM motor used for aircraft taxiing has been investigated. A 36 slots and 42-poles an out-runner PM machine is used for the studies. An analytical model able to predict the machine performance in terms of these losses has been proposed. By comparing with FE results, the validity of the analytical model has been proven. It has been shown that the multi-stranded conductors have influences on proximity effect due to changes in current distribution in a slot and thus, the resultant proximity losses not only depend on twisting or transposing the windings, but also on number of sub-strands implemented within a bundle conductor arrangement. Furthermore, efficiency can be improved at the design stage by investigating and adopting an appropriate configuration in terms of the cross sectional area/ number of turns of multi-strand bundle conductors.

ACKNOWLEDGEMENT

This work was partly supported by the “EU FP7 funding via the CleanSky JTI – Systems for Green Operations ITD”.

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